Reg No.:______ Name:_____

APJ ABDUL KALAM TECHNOLOGICAL UNIVERSITY

SIXTH SEMESTER B.TECH DEGREE EXAMINATION(S), DECEMBER 2019

Course Code: EE304

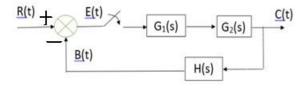
Course Name: ADVANCED CONTROL THEORY

Max. Marks: 100 Duration: 3 Hours

PART A

Answer all questions, each carries 5 marks. Marks

- Obtain the transfer function of a lead compensator with the help of an electrical (5) network.
- 2 Derive the transfer function of a PID Controller (5)
- 3 Derive a relation between state equation and transfer function for LTI system. (5)
- 4 Obtain the pulse transfer function for the system shown below. (5)



- With a neat diagram explain how the describing function analysis is used to (5) determine the stability of a system?
- What are jump response and limit cycles in connection with nonlinear systems? (5)
- 7 Explain with neat diagram, what is phase trajectory and phase portrait? (5)
- 8 Define positive definite and positive semi definite functions according to (5) Liapunov stability criteria, with suitable examples.

PART B

Answer any two full questions, each carries 10 marks.

- 9 a) Draw the bode-plot of lag compensator and obtain an expression for maximum (6) phase lag and corresponding frequency.
 - b) Explain turning of PID controller using Ziegler-Nichols tuning method. (4)
- Explain the procedure for design of a lag Compensator using Bode Plot with (10) suitable example
- 11 Consider a unity feedback system with open loop transfer function (10)

$$G(s) = \frac{k}{s(s+8)}$$

Design a lead compensator to meet the following specification:

- 1. Percentage peak overshoot is 9.5%
- 2. Natural frequency of oscillations 12 rad/sec
- 3. Velocity error constant ≥ 10

PART C

Answer any two full questions, each carries 10 marks.

12 a) A system is described by
$$\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ -4 & -4 \end{bmatrix} x(t)$$
 (5)

Determine state transition matrix for the system.

- b) Define controllability. Explain with a suitable example, how can we check the controllability of a system? (5)
- Derive the state model of the following transfer function in, (10)
 - (i) Controllable canonical form
 - (ii) Diagonal canonical form

$$\frac{y(s)}{u(s)} = \frac{5(s+2)}{s(s+1)(s+3)}$$

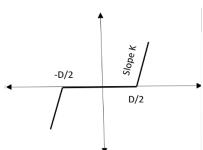
Examine the stability of the system with the following characteristic equation (10) using Jury's stability test.

$$z^4 - 1.2z^3 + 0.07z^2 + 0.3z - 0.08 = 0$$

PART D

Answer any two full questions, each carries 10 marks.

Identify the following non linearity and derive a describing function for the same (10)



16 Consider the following non linear differential equation.

$$\ddot{y} - \left(0.1 - \frac{10}{3}\dot{y}^2\right)\dot{y} + y + y^2 = 0$$

(10)

Find all singular points of the system, classify them and sketch the phase portrait in the neighbourhood of singular points.

- 17 a) Discuss any three non linearities present in nature. (6)
 - b) Investigate the stability of the following non-linear system using Liapunov (4) direct method

$$\dot{x}_1 = x_2$$
 $\dot{x}_2 = -x_1 - x_1^2 x_2$.
